

Chapter (9) Trigonometry

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1. (a) Solve $\sin x \cos x = 0.5 \tan x$ for $0^\circ \leq x \leq 180^\circ$.

[3]

(b) (i) Show that $\sec \theta - \frac{\sin \theta}{\cot \theta} = \cos \theta$.

[3]

(ii) Hence solve $\sec 3\theta - \frac{\sin 3\theta}{\cot 3\theta} = 0.5$ for $-\frac{2\pi}{3} \leq x \leq \frac{2\pi}{3}$, where θ is in radians,

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2. (a) (i) Show that $\sec \theta - \frac{\tan \theta}{\operatorname{cosec} \theta} = \cos \theta$.

[3]

(ii) Solve $\sec 2\theta - \frac{\tan 2\theta}{\operatorname{cosec} 2\theta} = \frac{\sqrt{3}}{2}$ for $0^\circ \leq \theta \leq 180^\circ$.

[3]

(b) Solve $2\sin^2\left(\phi + \frac{\pi}{3}\right) = 1$ for $0 \leq \phi \leq 2\pi$ radians.

[4]

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3. (a) (i) Show that $\frac{\operatorname{cosec} \theta - \cot \theta}{\sin \theta} = \frac{1}{1 + \cos \theta}$.

[4]

(ii) Hence solve $\frac{\operatorname{cosec} \theta - \cot \theta}{\sin \theta} = \frac{5}{2}$ for $180^\circ < \theta < 360^\circ$.

[2]

(b) Solve $\tan(3\phi - 4) = -\frac{1}{2}$ for $0 \leq \phi \leq \frac{\pi}{2}$ radians.

[3]

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4. (a) Solve $6\sin^2 x - 13 \cos x = 1$ for $0^\circ \leq x \leq 360^\circ$.

[4]

(b) (i) Show that, for $-\frac{\pi}{2} < y < \frac{\pi}{2}$, $\frac{4\tan y}{\sqrt{1+\tan^2 y}}$ can be written in the form $a \sin y$, where a is an integer.

[3]

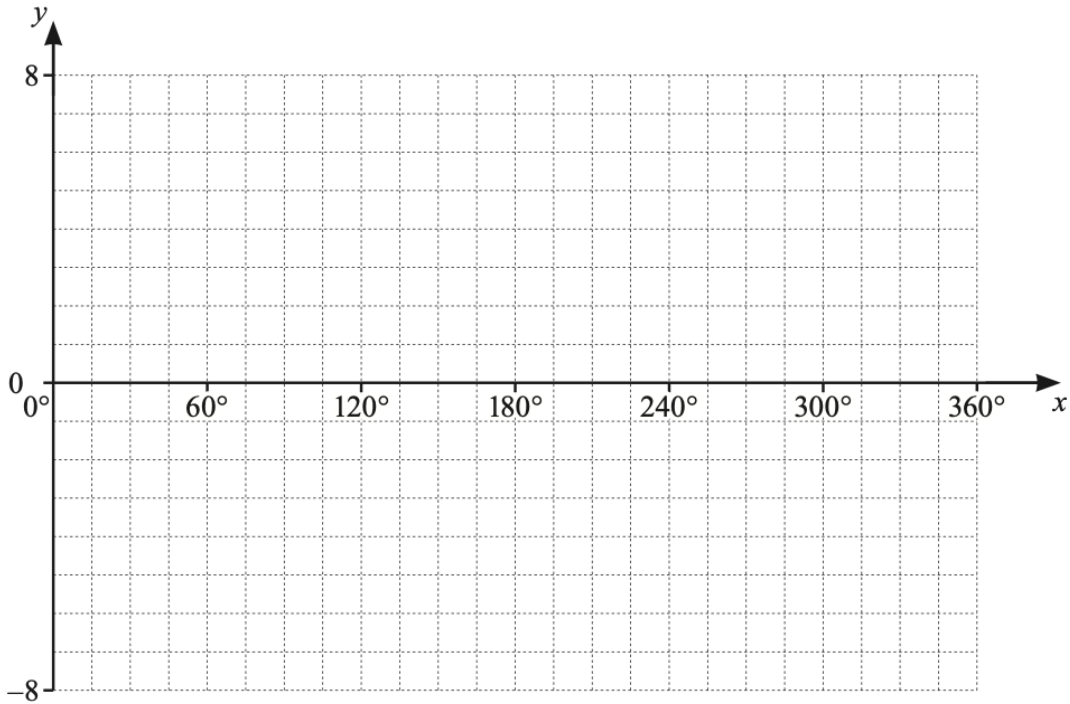
(ii) Hence, solve $\frac{4\tan y}{\sqrt{1+\tan^2 y}} + 3 = 0$ for $-\frac{\pi}{2} < y < \frac{\pi}{2}$ radians.

[1]

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5. The function f is defined, for $0^\circ \leq x \leq 360^\circ$, by $f(x) = 4 + 3\sin 2x$.

(i) Sketch the graph of $y = f(x)$ on the axes below.



(ii) State the period of f .

[3]

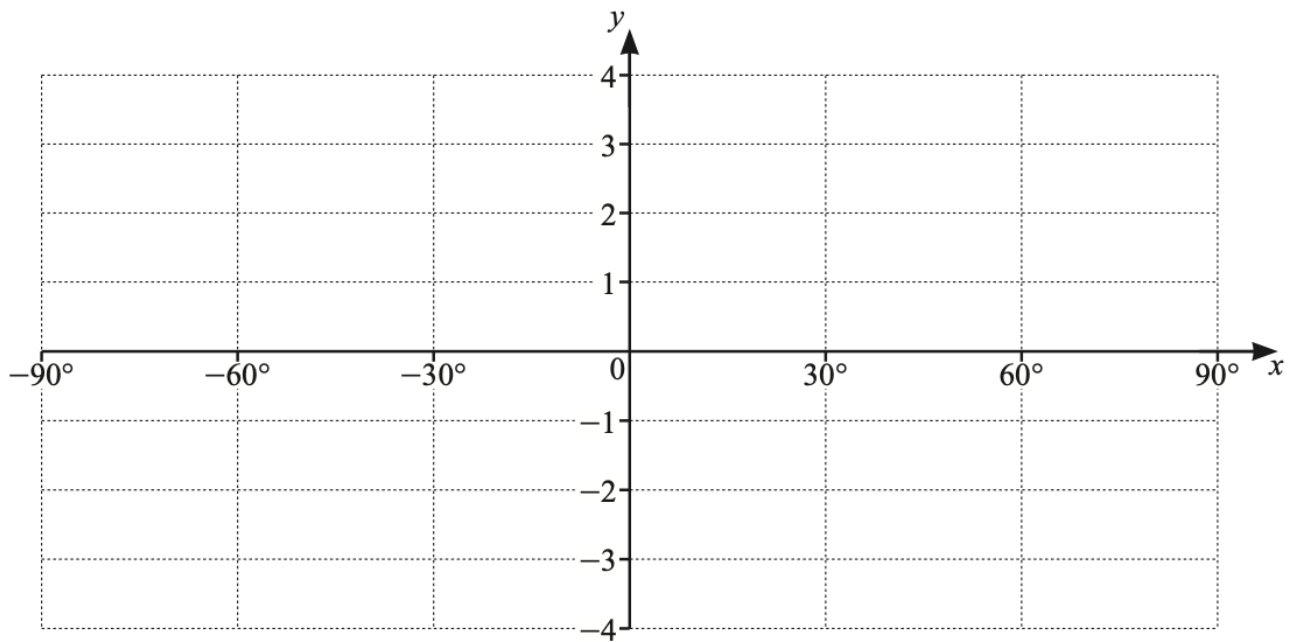
[1]

(iii) State the amplitude of f .

[1]

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6. (i) On the axes below, sketch the graph of $y = 2\cos 3x - 1$ for $-90^\circ \leq x \leq 90^\circ$.



[3]

(ii) Write down the amplitude of $2\cos 3x - 1$.

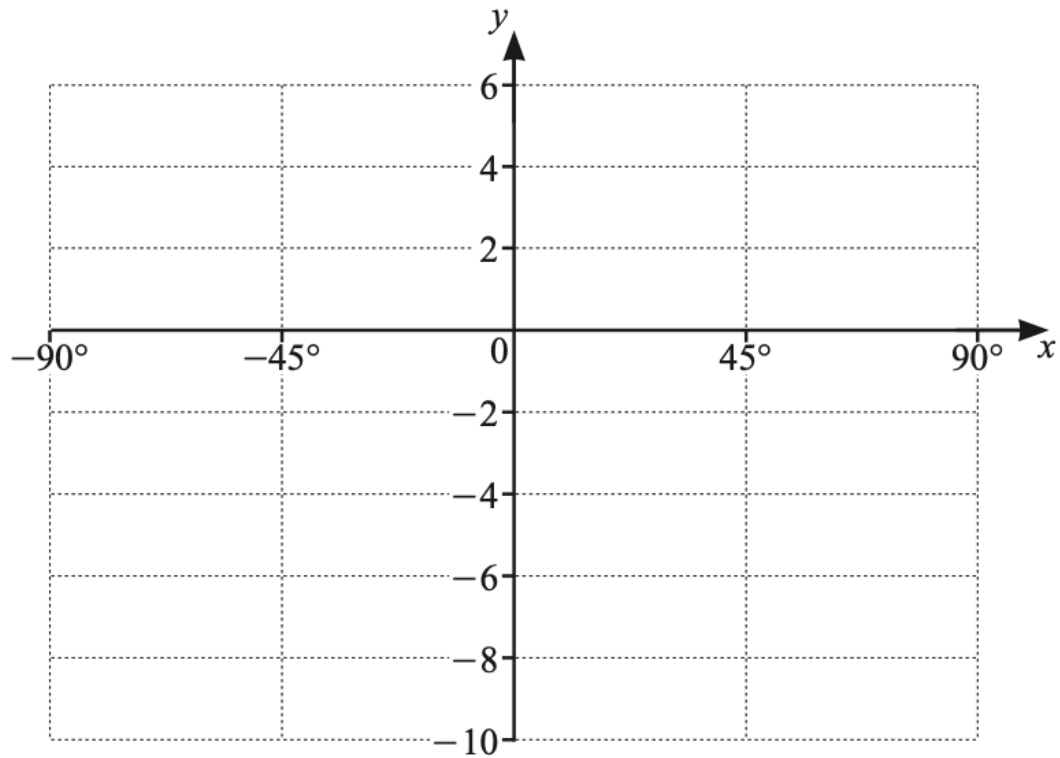
[1]

(iii) Write down the period of $2\cos 3x - 1$.

[1]

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7. (i) On the axes below, sketch the graph of $y = 5\cos 4x - 3$ for $-90^\circ \leq x \leq 90^\circ$.



[4]

- (ii) Write down the amplitude of y .

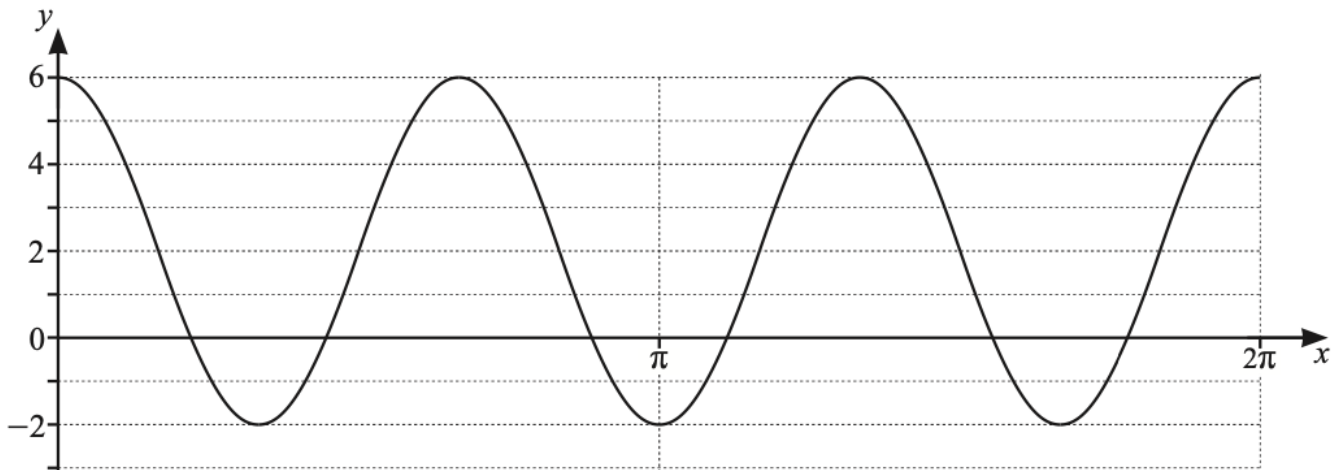
[1]

- (iii) Write down the period of y .

[1]

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8.



The figure shows part of the graph of $y = p + q \cos rx$. Find the value of each of the integers p , q and r .

$p =$

$q =$

$r =$

[3]

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9. (i) Show that $\frac{\tan x}{1+\sec x} + \frac{1+\sec x}{\tan x} = \frac{2}{\sin x}$.

[5]

(ii) Hence solve the equation $\frac{\tan x}{1+\sec x} + \frac{1+\sec x}{\tan x} = 1 + 3\sin x$ for $0^\circ \leq x \leq 180^\circ$.

[4]

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10. (i) Show that $\frac{\operatorname{cosec} x - \cot x}{1 - \cos x} = \operatorname{cosec} x$.

[3]

(ii) Hence solve $\frac{\operatorname{cosec} x - \cot x}{1 - \cos x} = 2$ for $0^\circ < x < 180^\circ$.

[2]